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# **Appointments**

2013- Stanford University

Professor of Physics

2010- Perimeter Institute for Theoretical Physics

Distinguished Research Chair

2008-2013 McGill University

Associate Professor of Computer Science Associate Member, Physics Department

2005-2013 McGill University

Canada Research Chair in the Physics of Information

2004-2008 McGill University

Assistant Professor of Computer Science Associate Member, Physics Department

2001-2004 California Institute of Technology

Sherman Fairchild Prize Postdoctoral Fellow

1999-2000 Exeter College, University of Oxford

Tutor in Physics

1989-1995 QNX Software Systems, Ltd.

Software developer and architect

# **Education**

1998-2001 University of Oxford

D. Phil. Physics (Rhodes Scholar)

Thesis: Distributing Quantum Information

Supervisor: Artur Ekert

1994-1998 McGill University

B. Sc. (Hon.) Mathematics and physics

Thesis: Symplectic Volumes of Spaces of Flat Connections

1989-1994 Sir Robert Borden High School

Valedictorian

### **Selected Honors and Awards**

- Canadian Association of Computer Science
  - 2011 Outstanding Young Computer Science Researcher Prize
- Canadian Institute for Advanced Research
  - 2010- Fellow of the Quantum Information Processing Program
  - **-** 2004-2009 **Scholar of the Quantum Information Processing Program**
- Alfred P. Sloan Foundation
  - 2007-2009 Sloan Research Fellowship in Computer Science
- University of Michigan Department of Electrical Engineering and Computer Science
  - 2006 General Dynamics Distinguished Lecturer
- Government of Canada
  - **•** 2005- Canada Research Chair in the Physics of Information
- Los Alamos National Laboratory
  - 2004 **J. Robert Oppenheimer Fellowship** (Declined)
- California Institute of Technology
  - 2001-2004 Sherman Fairchild Prize Fellowship
- University of Oxford
  - 1998-2001 Rhodes Scholarship
- McGill University

<b>•</b> 1998	Anne Molson Gold Medal (	Highest standing in	mathematics & physics)

- 1998 Horace Watson Medal and Prize (Highest standing in physics)
- 1997 **James Mathison Scholarship** (Academic standing in honours physics)
- 1996 **Stuart Foster Prize** (Academic standing in physics)
- 1994-1998 **Greville Smith Scholarship** (Tuition, expenses and stipend)
- For work at QNX software
  - 1996 EDN Magazine Innovation of the Year Finalist
  - 1995 **BYTE Magazine Editor's Award of Distinction**
  - 1995 Paris Real-Time Systems Exhibition Prix Fournisseur

# **Presentations**

#### **Public Lectures**

Perimeter Institute Public Lecturer
 Waterloo, 2009
 (One of six for 2009.)

Dawson College First Choice Lecturer
 Canadian Mathematical Society Public Lecturer
 Ottawa, 2008

(One of two per year, one for each biannual meeting)

#### **Invited Conference Presentations**

CIFAR Quantum Information Processing Workshop

QStart at the Hebrew University

US-India Advanced Studies Institute on Thermalization

Theory Canada 8

Conference in Honour of John Preskill's 60<sup>th</sup> Birthday

• Entangle This: Fields, Strings and Information

• 6<sup>th</sup> Annual Conference on Information Theoretic Security

International Congress of Mathematical Physics

Quantum Information School

Relativistic Quantum Information

Bits, Branes and Black Holes

Operator Structures in Quantum Information III

International Congress of Industrial and Applied Mathematics

Holographic Cosmology II

• Q. Info. in Quantum Gravity and Condensed Matter Physics

Quantum Information Processing

NATO Advanced School in Quantum Information

• Intl. Conf. on Quantum Information and Computation

Perspectives in High Dimensions

International Iran Summer School on Quantum Information

Random Matrices in Quantum Information

Sparse Random Structures

Operator Structures in Quantum Information

American Mathematical Society Winter Meeting

Black Holes and Quantum Physics

Quantum Theory and Symmetries 6

Quantum Information Processing

24<sup>th</sup> Texas Symposium on Astrophysics

CERN Black Hole Institute

Bellairs Workshop on Logic, Physics and Information

Gordon Research Conference on Quantum Information

IEEE Information Theory Workshop

- Southwest Quantum Information (SQuInT) Conference

LANL Classical and Quantum Information Workshop

Quantum Information Theory in Quantum Gravity

QuantumWorks Annual Meeting

28<sup>th</sup> Conference on Quantum Probability and Related Topics

Randomization of Quantum Systems

Dept. of Combinatorics and Optimization 40<sup>th</sup> Anniversary

Operator Structures in Quantum Information

Workshop on Quantum Cryptography and Computing

International Congress of Mathematical Physics

Symposium on Mathematical Physics

Benasque Center Quantum Information Workshop

CMS June Meeting

APS March Meeting

Quantum Information Processing

CIFAR Quantum Information Processing Workshop

Sherbrooke, 2013

Jerusalem, 2013

Bangalore, 2013

Sherbrooke, 2013

Pasadena, 2013

Madrid, 2012

Montreal, 2012

Aalborg, 2012

Capetown, 2012

Perimeter Institute, 2012

Santa Barbara, 2012

Banff, 2012

Vancouver, 2011

Perimeter Institute, 2011

Aspen, 2011

Singapore, 2011

Montreal, 2010

Stockholm, 2010

Cleveland, 2010

Kish Island, Iran, 2010

Perimeter Institute, 2010

BIRS, Banff, 2010

Fields Institute, 2009

Washington, DC, 2009

Perimeter Institute, 2009

Lexington, KY, 2009

Delhi, 2008

Vancouver, 2008

Geneva, 2008

Barbados, 2008

Montana, 2008

Porto, 2008

Santa Fe, 2008

Santa Fe, 2008

Perimeter Institute, 2007

Calgary, 2007

Guanajuato, 2007

Waterloo, 2007

Waterloo, 2007

BIRS, Banff, 2007

Fields Institute, 2006

Rio de Janeiro, 2006

Torun, Poland, 2006

Benasque, Spain, 2005

Waterloo, 2005

Los Angeles, 2005

Boston, 2005

Montebello, QC, 2004

 Quantum Communication, Measurement and Computing Glasgow, UK, 2004 ERATO Conference on Quantum Information Theory Kyoto, Japan, 2003 Ouantum Information Processing Berkeley, 2002 MSRI Workshop on Quantum Information Theory Berkeley, 2002 AMS Fall Meeting, Quantum Information Session Boston, 2002 AMS Winter Meeting, Quantum Information Session San Diego, 2002 Quantum Foundations in Light of Quantum Information Montreal, 2002 IEE Meeting on Nanotechnology and Quantum Computing Winchester, UK, 2000 Quantum Foundations in Light of Quantum Information Montreal, 2000 Quantum Communication, Measurement and Computing Capri, Italy, 2000

Quantum Algorithms and Information Processing Workshop Amsterdam, 2000

Selected Contributed Conference Presentations: (\*) indicates delivery by co-author

IEEE Conference on Computational Complexity: CCC (\*)
 Quantum Information Processing: QIP ("featured" talk)
 Quantum Information Processing (\*) ("featured" talk)
 ACM Symposium on Theory of Computing: STOC (\*)
 Quantum Information Processing (\*) (promoted to "invited")
 Quantum Information Processing (\*)
 Quantum Information Processing (\*)
 Quantum Information Processing (\*)

Quantum Information Processing
 IBM Yorktown, 2003

# **Seminars and Colloquia**

- Brandeis University, Physics Colloquium (2012)
- Brandeis University, Information Systems Seminar (2012)
- Caltech, Institute for Quantum Information Seminar (2011, 2002, 2001)
- Caltech, Information Science and Technology Seminar (2004)
- Cambridge University, Centre for Quantum Computation Seminar (2006)
- Centre de Recherches Mathematiques, Mathematical Physics Seminar (2012)
- ETH Zurich, *Physics Colloquium* (2013)
- IBM Research, *Physics of Information Seminar* (2003, 2002, 2000)
- Los Alamos National Lab, Quantum Lunch (2002, 2001, 2000)
- McGill University, Physics Colloquium (2006), High Energy Physics Seminar (2008)
- McGill University, Centre for Nonlinear Dynamics in Physiology and Medicine Seminar (2005)
- McGill University, Computer Science Colloquium (2004, 2001)
- MIT, Quantum Information Seminar (2012, 2011, 2007, 2005, 2002)
- MIT, Harvard-MIT String Theory Seminar (2012)
- Mittag-Leffler Institute, Seminar (2010)
- National University of Singapore, Centre for Quantum Technologies Colloquium (2009)
- Ohio State University, Physics Colloquium (2010)
- Perimeter Institute, Various Seminar Series (2010, 2007, 2006, 2003)
- Queen's University, Mathematics Colloquium (2007)
- Rutgers University, High-Energy Theory Seminar (2008)
- Stanford University, Institute for Theoretical Physics Seminar (2013, 2011, 2008)
- UC Berkeley, String Theory Seminar (2012)
- UC Berkeley, Theoretical Computer Science Seminar (2011)
- UC Berkeley, Physics Colloquium (2009)

- UC Berkeley, Quantum Information Seminar (2002)
- University of Bristol, Quantum Information Seminar (2006, 2002)
- University of British Columbia, Quantum Information Seminar (2011)
- University of Calgary, Institute for Quantum Information Science Seminar (2007)
- University of Michigan, General Dynamics Distinguished Lecture Series (2006)
- University of New Mexico, Center for Advanced Studies Seminar (2007, 2000)
- University of Ottawa, Mathematics Colloquium (2009)
- University of Sherbrooke, Condensed Matter Seminar (2007)
- University of Southern California, Communication Sciences Institute Seminar (2005)
- University of Toronto, Mathematics Colloquium (2010)
- University of Toronto, Quantum Information Seminar (2012, 2007, 2003)
- University of Washington, *Theoretical Computer Science Seminar* (2011)
- University of Waterloo, Institute for Quantum Computing Colloquium (2010, 2001)
- York University, Physics Colloquium (2005, 2013)

# **Publications**

### **Popular articles**

- Patrick Hayden. Entanglement as elbow grease. *Nature*. 474:41-42, 2011.
- Patrick Hayden. Putting certainty in the bank. Nature 436:633-634, 2005.

# Refereed journal articles (published and in press)

- Patrick Hayden, Kevin Milner and Mark Wilde. Two-message quantum interactive proofs and the quantum separability problem. arXiv:1211.6120, 2012. To appear in *Quantum Information and Computation*.
- Omar Fawzi, Patrick Hayden and Pranab Sen. From low-distortion norm embeddings to explicit uncertainty relations and efficient information locking. To appear in *Journal of the* ACM.
- Nicolas Dutil and Patrick Hayden. One-shot multiparty state merging. To appear in *IEEE Transactions on Information Theory*.
- Daniel Harlow and Patrick Hayden. Quantum computation versus firewalls. Journal of High Energy Physics (JHEP) 2013:85, 2013.
- Frederic Dupuis, Jan Florjanczyk, Patrick Hayden and Debbie Leung. The locking-decoding frontier for generic dynamics. *Proceedings of the Royal Society: Series A* 469:2159, 2013.
- Nima Lashkari, Douglas Stanford, Matthew Hastings, Tobias Osborne and Patrick Hayden.
   Towards the fast scrambling conjecture. Journal of High Energy Physics (JHEP) 2013:22, 2013.
- Patrick Hayden, Matthew Headrick and Alex Maloney. Holographic mutual information is monogamous. *Physical Review D* 87:046003, 2013.
- Mark Wilde, Patrick Hayden and Saikat Guha. Quantum trade-off coding for bosonic communication. *Physical Review A* 86:062306, 2012.

• Mark Wilde, Patrick Hayden, Francesco Buscemi and Min-Hsiu Hsieh. The information-theoretic costs of simulating quantum measurements. *Journal of Physics A: Mathematical and General*, 45:453001, 2012.

- Mark Wilde, Patrick Hayden and Saikat Guha. Information trade-offs for optical quantum communication. *Physical Review Letters*. 108:140501, 2012.
- Omar Fawzi, Patrick Hayden, Ivan Savov, Pranab Sen and Mark Wilde. Classical communication over a quantum interference channel. *IEEE Transactions on Information Theory.* 58(6):3670-3691, 2012.
- Paul Best, Marco Gualtieri and Patrick Hayden. Orbits of the centralizer of a linear operator. *Journal of Lie Theory.* 22(4):1039-1048, 2012.
- Patrick Hayden and Andreas Winter. Weak decoupling duality and quantum identification.
   IEEE Transactions on Information Theory. 58(7):4914-4929, 2012.
- Kamil Bradler, Patrick Hayden and Prakash Panangaden. Quantum communication in Rindler spacetime. *Communications of Mathematical Physics*. 312(2):361-398, 2012.
- Jon Yard, Patrick Hayden, Igor Devetak. Quantum broadcast channels. *IEEE Transactions on Information Theory*. 57(10):7147-7162, 2011.
- Nicolas Dutil and Patrick Hayden. Assisted entanglement distillation. *Quantum information and computation*. 11:0496-0520, 2011.
- David Avis, Patrick Hayden and Mark Wilde. Leggett-Garg inequalities and the geometry of the cut polytope. *Physical Review A*, 82:030102, 2010.
- Kamil Bradler, Patrick Hayden, Dave Touchette and Mark Wilde. Trade-off capacities of the quantum Hadamard channels. *Physical Review A*, 81:062312, 2010.
- Kamil Bradler, Nicolas Dutil, Patrick Hayden and Abubakr Muhammad. Conjugate degradability and the quantum capacity of cloning channels. *Journal of Mathematical Physics*, 51:072201, 2010.
- Frédéric Dupuis and Patrick Hayden. A father protocol for quantum broadcast channels. *IEEE Transactions on Information Theory*, 56(6):2946-2956, 2010.
- Anura Abeyesinghe, Igor Devetak, Patrick Hayden and Andreas Winter. The mother of all protocols: Restructuring quantum information's family tree. *Proceedings of the Royal Society* of London A, 465(2108):2537-2563, 2009.
- Kamil Bradler, Patrick Hayden and Prakash Panangaden. Private information via the Unruh effect. *Journal of High Energy Physics (JHEP)*, 08(174), 2009.
- David Avis, Patrick Hayden and Ivan Savov. Distributed compression and multiparty squashed entanglement. *Journal of Physics A*, 41:115301, 2008.
- Jon Yard, Igor Devetak and Patrick Hayden. Capacity theorems for quantum multiple access channels - Classical-quantum and quantum-quantum capacity regions. *IEEE Transactions on Information Theory*, 54(7)3091-3113, 2008.
- Andreas Winter and Patrick Hayden. Counterexamples to the maximal p-norm multiplicativity conjecture for all p>1. *Communications of Mathematical Physics*, 284(1):263-280, 2008.

Cory Dean, Benjamin Piot, Patrick Hayden, Sankar Das Sarma, Guillaume Gervais, Loren
Pfeiffer and Ken West. Contrasting behavior of the 5/2 and 7/3 fractional quantum Hall effect
in a tilted field. *Physical Review Letters*, 101:186806, 2008.

- Harry Buhrman, Matthias Christandl, Patrick Hayden, Hoi-Kwong Lo and Stephanie Wehner.
   Possibility, impossibility, and cheat sensitivity of quantum-bit string commitment. *Physical Review A*, 78:022316, 2008.
- Cory Dean, Benjamin Piot, Patrick Hayden, Sankar Das Sarma, Guillaume Gervais, Loren Pfeiffer and Ken West. Intrinsic gap of the v=5/2 fractional quantum Hall state. *Physical Review Letters*, 100:146803, 2008.
- Patrick Hayden, Michal Horodecki, Andreas Winter and Jon Yard. A decoupling approach to the quantum capacity. *Open Systems and Information Dynamics*, 15:7-19, 2008.
- Patrick Hayden, Peter Shor and Andreas Winter. Random quantum codes from Gaussian ensembles and an uncertainty relation. Open Systems and Information Dynamics, 15:71-89, 2008.
- Patrick Hayden and John Preskill. Black holes as mirrors: Quantum information in random subsystems. *Journal of High Energy Physics (JHEP)*, 09:120, 2007.
- David Avis, Patrick Hayden and Ivan Savov. Distributed compression and multiparty squashed entanglement. *Journal of Physics A*, 41:115301, 2008.
- Harry Buhrman, Matthias Christandl, Patrick Hayden, Hoi-Kwong Lo and Stephanie Wehner.
   Security of quantum bit string commitment depends on the information measure. *Physical Review Letters*, 97:250501, 2006.
- Anura Abeyesinghe, Patrick Hayden, Graeme Smith and Andreas Winter. Optimal superdense coding of entangled states. *IEEE Transactions on Information Theory*, 52(8):3635-3641, 2006.
- Patrick Hayden, Debbie Leung and Andreas Winter. Aspects of generic entanglement. *Communications of Mathematical Physics*, 265(1)95-117, 2006.
- Charlene Ahn, Andrew Doherty, Patrick Hayden and Andreas Winter. On the distributed compression of quantum information. *IEEE Transactions on Information Theory*, 52(10):4349-4357, 2006.
- Stephen D. Bartlett, Patrick Hayden and Robert W. Spekkens. Random subspaces for encryption based on a private shared Cartesian frame. *Physical Review A*, 72:052329, 2005.
- Sumit Daftuar and Patrick Hayden. Quantum state manipulations and the Schubert calculus. *Annals of Physics*, 315(1)80-122, 2005.
- Charles Bennett, Patrick Hayden, Debbie Leung, Peter Shor, and Andreas Winter. Remote preparation of quantum states. *IEEE. Transactions on Information Theory*, 51(1)56-74, 2005.
- Patrick Hayden and Christopher King. Correcting quantum channels by measuring the environment. Quantum Information and Computation, 5(2)156-160, 2005.
- Patrick Hayden, Debbie Leung and Graeme Smith. Multiparty data hiding of quantum information. *Physical Review A*, 71:062339, 2005.
- Aram Harrow, Patrick Hayden and Debbie Leung. Superdense coding of quantum states. *Physical Review Letters*, 92:187901, 2004.

• Patrick Hayden, Debbie Leung, Peter Shor, and Andreas Winter. Randomizing quantum states: Constructions and applications. *Communications of Mathematical Physics*, 250(2):371-391, 2004.

- Patrick Hayden, Richard Jozsa, Denes Petz and Andreas Winter. Conditions for equality in the strong subadditivity inequality for quantum entropy. *Communications of Mathematical Physics*, 246(2):359-374, 2004.
- Anura Abeyesinghe and Patrick Hayden. Generalized remote state preparation: Trading cbits, qubits and ebits in quantum communication. *Physical Review A*, 68:062319, 2003.
- David D. DiVincenzo, Patrick Hayden and Barbara M. Terhal. Hiding quantum data. *Foundations of Physics*, 33(11):1629-164, 2003.
- Wim van Dam and Patrick Hayden. Embezzling entangled quantum states (Universal entanglement transformations without communication). *Physical Review A*, 67:060302, 2003.
- Patrick Hayden and Andreas Winter. On the communication cost of entanglement transformations. *Physical Review A*, 67:012326, 2003.
- Patrick Hayden, Richard Jozsa and Andreas Winter. Trading quantum and classical resources in quantum data compression. *Journal of Mathematical Physics*, 43(9):4404-4444, 2002.
- Howard Barnum, Patrick Hayden, Richard Jozsa and Andreas Winter. On the reversible extraction of information from a quantum source. *Proceedings of the Royal Society of London A*, 457(2012):2019-2039, 2001.
- Simon C. Benjamin and Patrick Hayden. Comment on "Quantum games and quantum strategies". *Physical Review Letters*, 87:069801, 2001.
- Simon C. Benjamin and Patrick Hayden. Multiplayer quantum games. *Physical Review A*, 64:030301, 2001.
- Artur Ekert, Patrick Hayden, Hitoshi Inamori, and Daniel Oi. What is quantum computation?
   International Journal of Modern Physics A, 16(20):3335-3363, 2001.
- Patrick Hayden, Michal Horodecki, and Barbara M. Terhal. The asymptotic entanglement cost of preparing a quantum state. *Journal of Physics* A, 34(35):6891-6898, 2001.
- David Deutsch and Patrick Hayden. Information flow in entangled quantum systems.
   Proceedings of the Royal Society of London A, 456(1999):1759-1774, 2000.
- Artur Ekert, Marie Ericsson, Patrick Hayden, Hitoshi Inamori, Jonathan Jones, Daniel Oi, and Vlatko Vedral. Geometric quantum computation. *Journal of Modern Optics*, 47(14/15):2501-2513, 2000.

#### Refereed conference proceedings

- Mark Wilde, Olivier Landon-Cardinal and Patrick Hayden. Towards efficient decoding of classical-quantum polar codes. To appear in Proceedings of the 8<sup>th</sup> Conference on Theory of Quantum Computation, Communication and Cryptography (TQC), 2013.
- Patrick Hayden, Kevin Milner and Mark Wilde. Two-message quantum interactive proofs and the quantum separability problem. *Proceedings of the IEEE Conference on Computational Complexity (CCC)*, pp. 156-167, 2013.

 Omar Fawzi, Patrick Hayden, Ivan Savov, Pranab Sen and Mark Wilde. Quantum interference channels. *Proceedings of the 49<sup>th</sup> Allerton Conference on Communication, Control, and Computing*, IEEE, pp. 609-616, 2011.

- Omar Fawzi, Patrick Hayden and Pranab Sen. From low-distortion embeddings to explicit uncertainty relations and efficient information locking. *Proceedings of the 43<sup>rd</sup> ACM* Symposium on Theory of Computing (STOC 2011), ACM, pp. 773-782, 2011.
- Patrick Hayden. Concentration of measure effects in quantum information. In Quantum Information Science and its Contributions to Mathematics, *Proceedings of Symposia in Applied Mathematics*, vol. 68. American Mathematical Society, pp. 3-12, 2010.
- David Avis, Patrick Hayden and Ivan Savov. Multiparty distributed compression of quantum information. In *Proceedings of the Second International Conference on Quantum, Nano and Micro Technologies*. IEEE, 2008. (Best paper award.)
- Jon Yard, Patrick Hayden and Igor Devetak. Quantum broadcast channels. In Proceedings of the ERATO Conference on Quantum Information Science, Tokyo, Japan, 2005.
- Jon Yard, Igor Devetak, Patrick Hayden. Capacity theorems for quantum multiple access channels In *Proceedings of the 2005 IEEE Symposium on Information Theory, Adelaide,* Australia, pp. 884-888, 2005.
- Jon Yard, Igor Devetak, Patrick Hayden. Sending classical and quantum information over quantum multiple access channels. In *Proceedings of the ninth Canadian Workshop on Information Theory, Montreal, Canada.* pp. 387-390, 2005.
- Patrick Hayden. Entanglement in random subspaces. In *Proceedings of the Seventh International Conference on Quantum Communication, Measurement and Computing.*American Institute of Physics. pp. 226-229, 2004.
- Artur Ekert, Patrick Hayden, and Hitoshi Inamori. Basic concepts in quantum computation. In R. Kaiser, C. Westbrook, and F. David, editors, *Proceedings of the 1999 Les Houches* summer school on "Coherent Matter Waves", volume 72, pp. 661-703, 2001.

#### Refereed book chapters

• P. Hayden. Capacities enhanced by entanglement. In *Encyclopedia of Mathematical Physics*, eds. J.-P. Francoise, G.L. Naber and S.T. Tsou, pp. 418-424. Elsevier, 2006.

#### Preprints on arXiv.org

- Kevin Milner, Gus Gutoski, Patrick Hayden and Mark Wilde. Quantum interactive proofs and the complexity of entanglement detection. arXiv:1308.5788, 2013. Submitted to *Theory of Computing*.
- Saikat Guha, Patrick Hayden, Hari Krovi, Seth Lloyd, Cosmo Lupo, Jeffrey Shapiro, Masahiro Takeoka and Mark Wilde. Quantum enigma machines and the locking capacity of a quantum channel. arXiv:1307.5368, 2013. Submitted to *Physical Review X*.
- Patrick Hayden and Alex May. Summoning information in spacetime, or where and when can a qubit be?, arXiv:1210.0913, 2012. Submitted to *Physical Review Letters*.
- Patrick Hayden. The maximal p-norm multiplicativity conjecture is false. arXiv:0707.3291, 2007.

• Robin Blume-Kohout and Patrick Hayden. Accurate quantum state estimation via "Keeping the experimentalist honest." arXiv:quant-ph/0603116, 2006.

- Wim van Dam and Patrick Hayden. Renyi-entropic bounds on quantum communication. arXiv:quant-ph/0204093, 2002.
- Patrick Hayden, Barbara M. Terhal, and Armin Uhlmann. On the LOCC classification of bipartite density matrices. arXiv:quant-ph/0011095, 2000.

# **Patents**

• Patrick M. Hayden and Robin Burgener. Window Kernel. United States Patent 5,745,759. Granted April 28, 1998.